Strong Deformation of Ferrofluid-Filled Elastic Alginate Capsules in Inhomogenous Magnetic Fields

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Supporting Information

ABSTRACT: We present a new system based on alginate gels for the encapsulation of a ferrofluid drop, which allows us to create millimeter-sized elastic capsules that are highly deformable by inhomogeneous magnetic fields. We use a combination of experimental and theoretical work in order to characterize and quantify the deformation behavior of these ferrofluid-filled capsules. We introduce a novel method for the direct encapsulation of unpolar liquids by sodium alginate. By adding 1-hexanol to the unpolar liquid, we can dissolve sufficient amounts of CaCl₂ in the resulting mixture for ionotropic gelation of sodium alginate. The addition of polar alcohol molecules allows us to encapsulate a ferrofluid as a single phase rather than an emulsion without impairing ferrofluid stability. This encapsulation method increases the amount of encapsulated magnetic nanoparticles resulting in high deformations of approximately 30% (in height-to-width ratio) in inhomogeneous magnetic field with magnetic field variations of 50 mT over the size of the capsule. This offers possible applications of capsules as actuators, switches, or valves in confined spaces like microfluidic devices. We determine both elastic moduli of the capsule shell, Young’s modulus and Poisson’s ratio, by employing two independent mechanical methods, spinning capsule measurements and capsule compression between parallel plates. We then show that the observed magnetic deformation can be fully understood from magnetic forces exerted by the ferrofluid on the capsule shell if the magnetic field distribution and magnetization properties of the ferrofluid are known. We perform a detailed analysis of the magnetic deformation by employing a theoretical model based on nonlinear elasticity theory. Using an iterative solution scheme that couples a finite element/ boundary element method for the magnetic field calculation to the solution of the elastic shape equations, we achieve quantitative agreement between theory and experiment for deformed capsule shapes using the Young modulus from mechanical characterization and the surface Poisson ratio as a fit parameter. This detailed analysis confirms the results from mechanical characterization that the surface Poisson ratio of the alginate shell is close to unity, that is, deformations of the alginate shell are almost area conserving.

INTRODUCTION

Ferrofluids contain dispersed magnetizable nanoparticles, which are long-time stable and exhibit superparamagnetic behavior. Ferrofluids can be actuated by magnetic fields and have various technical and medical applications. In many applications it is of interest to prevent a ferrofluid from interaction with its environment, especially considering its corrosive effects on metals. This can be achieved by encapsulation of a ferrofluid drop with a thin protective shell made, for example, from a gel or soft elastic material. The result is an elastic capsule with a stable ferrofluid droplet inside. The elastic shell protects the inner fluid from direct interaction with the environment but it can be deformed by various external forces. Elastic capsules are stable under uniform pressure up to a buckling threshold. Buckling indentations can also be induced by point forces and capsules can be deformed in hydrodynamic flow. Other deformation techniques include compression between parallel plates or in a spinning drop apparatus, or pendant capsule elastometry. These mechanical deformation techniques can be employed to determine the elastic moduli of capsule shells. Whereas these deformation techniques require direct mechanical interaction with the capsules, deformation can also be driven by external electric or magnetic fields if the capsules are filled by a dielectric liquid or ferrofluid or if the shell itself contains magnetizable particles. In particular, we demonstrate in this paper that magnetic actuation and mechanical characterization of a capsule filled with a ferrofluid is possible by deformation in a magnetic field.

The aim of this work is the encapsulation of a stable ferrofluid drop with high magnetic nanoparticle concentration in order to achieve strong deformation in an external magnetic field and a quantitative understanding of the deformation behavior by comparison to theoretical predictions based on nonlinear elasticity theory. Encapsulation of stable ferrofluids was achieved in refs 21 and 22 for example, for magnetic...
resonance imaging.22 Ferrofluid concentration inside the capsules were low, however, such that there are no reports on actuation and deformation properties in magnetic fields. On the other hand, magnetic deformation of capsules filled with magnetic particles was reported in refs 23 and 24 these magnetic particles, however, aggregated and did not remain in a stable ferrofluid state. The aim of this work is a reliable capsule system, into which a stable ferrofluid can be loaded at high concentration such that it can strongly deform in magnetic fields, which is important for possible applications of capsules as actuators, switches, or valves.

We present a new method to achieve stable ferrofluid encapsulation at high concentrations. Generally, encapsulation of magnetic nanoparticles in a stable dispersion in the liquid core is a difficult task. Here, we use alginate gel as shell material. Because of its mild gelation conditions, nontoxicity, and biocompatibility, it is a widely used encapsulation material.24−29 Sodium alginate is soluble in water, and ionotropic gelation takes place upon contact with bi- or trivalent cations;30,31 usually, calcium is used for the gelation. Magnetic nanoparticles, which are sterically stabilized by amphiphiles such as lauric acid or electrostatically stabilized, destabilize and flocculate in the presence of calcium ions if both ions and nanoparticles are in the aqueous phase in the liquid core of the capsule.29 To reduce this effect oil-soluble magnetic particles can be used, which are encapsulated in an oil in water emulsion, where calcium is solved in the aqueous emulsion phase.28 In previous work, we showed that encapsulation of a stable ferrofluid is possible with this technique and that a significant deformation in magnetic fields can be achieved.32 The deformation was, however, limited to approximately 10% because magnetic nanoparticles are only contained in the oil emulsion phase, whereas a certain amount of unmagnetizable aqueous emulsion phase is needed to solve calcium ions. In order to further increase the magnetic nanoparticle content in the liquid core of the capsule we use 1-hexanol as a solvent with high polarity but low water-solubility to dissolve significant amounts of calcium chloride. We mix 1-hexanol with chloroform as a second solvent because the magnetite nanoparticles are not dispersable in pure 1-hexanol. Chloroform also increases the density of the liquid core which improves experimental handling of the capsules. The general principle of using 1-hexanol as an additive can be extended to a variety of oils. The advantage of direct oil encapsulation concerning the encapsulation of ferrofluids is the higher magnetic content, which leads to higher deformation in the same magnetic field. In emulsion-based systems the need for a second phase reduces the overall nanoparticle concentration and thus the reaction to magnetic fields.

The ferrofluid-filled capsule represents a magnetic dipole. In order to achieve strong deformation we use inhomogeneous magnetic fields, which are easily realizable and result in a net force onto the ferrofluid-filled capsule. We use this net force to deform the capsule by pushing the flexible particle against the bottom wall of the cuvette. In principle, deformation and shape transitions are also possible in homogeneous magnetic fields, which tend to stretch the capsule in order to increase the dipole moment.18 For a quantitative understanding of the deformation behavior we measure the magnetic field distribution, calculate the magnetic properties of the ferrofluid from the nanoparticle size distribution and compare the experimental capsule shapes to theoretical shapes calculated using nonlinear elasticity theory by a coupled finite element method (FEM) for the elastic problem and a boundary element method (BEM) for the magnetic field calculation. This enables us to also obtain additional information not easily accessible in experiments such as a detailed picture of the magnetic field distribution and the elastic stress distribution in the capsule, which are important, for example, to predict capsule rupture because of magnetic deformation.

## MATERIALS AND METHODS

### Preparation of the Magnetic Nanoparticles.

Preparation of Capsules. We encapsulate a mixture of chloroform and 1-hexanol (7:3) containing dispersed magnetite nanoparticles with a mass concentration \( c_m = 516 \text{ g/mol} \) in an alginate gel shell. Initially, calcium chloride is dissolved in the 1-hexanol/chloroform mixture (by volume 3:7) in order to perform the alginate gelation. Two additional surfactants stabilizing the nanoparticles, oleic acid, and oleylamine, also accelerate the gelation and are added with 1% (volume percent) each to improve the process.

The high chloroform content requires to adjust the capsule preparation process, which is normally done by dripping one component, either sodium alginate or calcium chloride solution, directly (from air) into the other liquid. Because of the high chloroform content of 70 %V, dripping of the 1-hexanol/chloroform mixture containing the calcium chloride from air into the alginate solution is not feasible because the mixture spreads on the interface. Instead we first overlay a cylinder which is filled to 7/8 with sodium alginate solution (1% by weight) with distilled water and form a droplet of the 1-hexanol/chloroform mixture in the water layer using a capillary, see Figure 1. The droplet then falls through the interface between water and alginate solution without spreading. Within the alginate solution, the calcium chloride dissolved in the 1-hexanol/chloroform droplet starts the gelation. In order to avoid contact with

![Figure 1. Procedure for the production of ferrofluid-filled capsules.](364x111 to 524x336)

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13535
the glass surface a seal (shown in grey in Figure 1) can be placed over the opening and the cylinder can be turned for 30 s.

The capsules are washed with water to stop the polymerisation and placed in saturated sodium alginate solution. This lowers the elastic moduli of alginate systems and thus lead to capsules that are easier to deform.

**Experimental Setup for Mechanical Characterization.** For mechanical characterization of the capsule shells we use two methods, compression between parallel plates and deformation in a spinning drop apparatus. Combination of the results from both measurements will enable us to determine both the two-dimensional Young modulus \( Y_{12} \) and the surface Poisson ratio \( \nu \).

In the compression method a capsule is placed between two parallel plates and the force is measured as a function of the displacement. A sketch of the method is shown in the Supporting Information. Compression between parallel plates was performed with the DCAT11 tensiometer (DataPhysics Instruments GmbH) with the software SCAT. The compression speed was set to 0.02 mm/s.

In a spinning drop apparatus, a capsule is placed in a capillary filled with a liquid of higher density \( \rho \) and monitored with a camera (see Supporting Information). During rotation of the capillary, the capsule moves to the horizontal axis of the capillary and deforms. The deformation is measured as a function of angular rotation frequency. For the spinning capsule experiments, we used the SVT 20 of the DataPhysics Instruments GmbH. We used Fluorinert 70 (FC 70) as outer phase because of its high density. The initial undeformed (quiescent) capsule state was recorded at 2000 rpm.

Capsule radii were determined by image analysis of capsule photos (see Supporting Information). For the shell thickness this image analysis could not be used because of the small thickness. Thus, scanning electron microscopy (SEM) measurements were performed to estimate the shell thickness. From the images shown in the Supporting Information, it can also be concluded that the nanoparticles were not incorporated in the shell.

**Elastic and Magnetic Model for Deformation.** In order to model the magnetic deformation of a capsule we need an elastic material model for the capsule shell and a magnetic model for the calculation of the magnetic forces. To calculate the shape of a deformed capsule, we use a small strain nonlinear shell theory with a Hookean elastic law.\(^{1,4}\) In our model, we assume a very thin, effectively two-dimensional elastic shell and rotational symmetry. We also assume that the capsule attains a perfectly spherical stress-free reference shape with rest radius \( R_0 \) during the polymerization process. All these assumptions hold to a good approximation in the experimental realization. Once the elastic shell is polymerized, there is no exchange of fluid between the inner phase and the outer phase possible anymore, at least under the employed experimental conditions and during magnetic deformation. So the volume \( V_0 \) of the capsule remains constant. The capsule is then deformed by a hydrostatic pressure caused by the density difference \( \Delta \rho \) between the inner phase and the outer phase. In the presence of an additional magnetic field, the magnetic stress caused by the ferrofluid deforms the capsule as well. We consider capsules which sink to the bottom of a cuvette where also the magnetic deformation takes place, and both gravity and magnetic forces press the capsule against the bottom wall of the cuvette. In a steady state without motion, the fluid can only exert normal forces on the surface. The normal forces caused by the ferrofluid are given by

\[
\mathbf{f}_{n}(r, z) = \mu_0 J_0^H \int_{0}^{H(r, z)} M(r, z) dH(r, z) + \frac{\mu_0}{2} M^2(r, z)
\]

(1)

\( M \) and \( M_0 \) are absolute value and normal component of the magnetization \( \mathbf{M} \), \( H \) the magnetic field, and we use cylindrical coordinates \( r \) and \( z \); for a ferrofluid we can safely assume that \( \mathbf{M} \) and \( \mathbf{H} \) are parallel. The deformed shape of the capsule can be calculated by using a system of six nonlinear differential equations, the shape equations, see ref 9 for a derivation and the Supporting Information for more details.

There are two material parameters, the two-dimensional Young modulus \( Y_{12} \) and the surface Poisson ratio \( \nu \), that enter the theoretical model. These parameters are obtained from the mechanical characterization of the capsule by plate compression and spinning capsule deformation as explained below in the Experiments and Results section. Moreover, the rest radius \( R_0 \) of the initially spherical capsule and the thickness \( h \) of the shell are needed. The thickness \( h \) determines the bending modulus via \( E_b = Y_{12}h^2/12(1 - \nu^2) \) and \( R_0 \) determines the initial rest shape with respect to which elastic strains and stresses are obtained and the fixed volume \( V_0 \). Moreover, the density difference \( \Delta \rho \) between the interior and exterior liquid phases is needed for the hydrostatic pressure.

In addition, the effective interface tension \( \gamma \) between the inner liquid phase and the elastic shell and between the shell and the outer liquid phase has to be estimated, but is very difficult to be measured. Generally, we expect solid–liquid surface tensions to be smaller than liquid–liquid surface tensions.\(^2\) Because the shell can still contain pores leading to liquid–liquid contact, we expect the interface tension \( \gamma \) to be lower than but similar to the interfacial tension between outer and inner liquid. The interfacial tension of a similar system without elastic shell and without nanoparticles inside was determined to be 14.6 mN/m by pendant drop tensiometry. The presence of surfactants from the synthesis of the nanoparticles as well as the elastic shell should lower the interface tension below this value. In addition, it should be mentioned that the interfacial tension of the ferrofluid is probably increasing for increasing external magnetic field as Akhami et al. observed.\(^3\) We expect \( \gamma \approx 10 \pm 4 \) mN/m to be a valid average value.

The parameter values that are used for the numerical calculation of capsule shapes are summarized in Table 1. The surface Poisson ratio deviates slightly from the value measured in the experiment (eq 11). This will be discussed below in the Experiments and Results section.

Finally, the exact distribution of the applied inhomogeneous magnetic field and the magnetic properties of the ferrofluid, that is, its magnetization curve \( M = M(H) \) have to be known as well in order to calculate the magnetic forces (eq 1), see following sections.

<table>
<thead>
<tr>
<th>name</th>
<th>symbol</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>2D Young’s modulus</td>
<td>( Y_{12} )</td>
<td>0.186 N/m</td>
</tr>
<tr>
<td>surface Poisson ratio</td>
<td>( \nu )</td>
<td>0.946</td>
</tr>
<tr>
<td>shell thickness</td>
<td>( h )</td>
<td>3 ( \mu m )</td>
</tr>
<tr>
<td>radius</td>
<td>( R_0 )</td>
<td>0.903–1.044 mm</td>
</tr>
<tr>
<td>density difference</td>
<td>( \Delta \rho )</td>
<td>0.24 g/cm(^2)</td>
</tr>
<tr>
<td>surface tension</td>
<td>( \gamma )</td>
<td>10 mN/m</td>
</tr>
</tbody>
</table>
Magnetic Field. We used a Hall probe to measure the magnetic field depending on the position and the applied current \( I \) in the coil (see Figure 2). The capsules are very small in relation to the size of the coil and the conical iron core, so the radial component of the magnetic field can be neglected. In addition, the \( z \)-component of the field is nearly constant in radial direction over the capsule size and thus only depends on the \( z \)-coordinate. In the numerical calculations we use a fit to the measured external magnetic field with a Langevin function to model the dependence on current \( I \) and a hyperbolic function for the dependence on height \( z \)

\[
B_z(z, I) = a \coth(b I) - \frac{1}{b I} \left( \frac{d_1}{z - b_2} + c_1 \right)
\]

(2)

with fit parameters \( a = 4.647, b_1 = 0.332 \, \text{A}^{-1}, a_z = 286.7 \times 10^{-6} \, \text{mT}, b_z = -1.104 \times 10^{-3} \, \text{m}, \) and \( c_1 = 10.86 \times 10^{-3} \, \text{T}. \) A plot of the fit curve together with the measured magnetic field is shown in the Supporting Information. The fit describes the magnetic field with an error below 1\% in the neighborhood of the capsule.

Magnetization Curve. The magnetization curve of the ferrofluid is calculated from the particle size distribution of the magnetite nanoparticles. The particle size distribution is obtained from dynamic light scattering (see Supporting Information) and given in Table 2, where the relative frequency \( n_i \) of particle diameters \( d_i = 5-14 \, \text{nm} \) are given. The particle size distribution has a maximum around \( d = 7-8 \, \text{nm} \).

<table>
<thead>
<tr>
<th>( d_i [\text{nm}] )</th>
<th>( n_i [%] )</th>
<th>( d_i [\text{nm}] )</th>
<th>( n_i [%] )</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>2.0</td>
<td>10</td>
<td>8.6</td>
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<td>6</td>
<td>14.1</td>
<td>11</td>
<td>7.6</td>
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<td>7</td>
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<td>8</td>
<td>23.9</td>
<td>13</td>
<td>3.8</td>
</tr>
<tr>
<td>9</td>
<td>16.1</td>
<td>14</td>
<td>2.4</td>
</tr>
</tbody>
</table>

Table 2. Particle Size Distribution: Relative Frequency \( n_i \) of Particle Diameter \( d_i \)

According to ref 1 the magnetization \( M \) as a function of the field strength \( H \) is then given by

\[
M(H) = M_s \sum_i n_i (d_i - d) \coth(x) - 1/\mu_s \int \frac{d_H M_s H x}{6} (d_i - d)^2 \sum_i n_i d_i^3
\]

(3)

with the Langevin function \( L(x) = \coth(x) - 1/x \), \( M_s = 34650 \, \text{A m}^{-1} \) is the saturation magnetization of the magnetite particles without sterical stabilization and \( M_0 = 446000 \, \text{A m}^{-1} \) denotes the bulk magnetization of magnetite. The diameters of the nanoparticles are reduced by \( d_2 \) because the crystal order of the outer surface layer of magnetite is disturbed by the dispersing agent. This lowers also the effective saturation magnetization of the ferrofluid. Following ref 1 we use \( d_2 = 1.66 \, \text{nm} \). The resulting magnetization curve is shown in Figure 3.

Numerical Procedure. The calculation of the magnetic field inside the capsule and the ferrofluid is done numerically by a coupled FEM/BEM. The shape of the elastic shell and the magnetic field inside the capsule form a coupled problem that has to be solved self-consistently: changes in the shape of the elastic shell cause changes in the magnetic field distribution inside the capsule, which, in turn, changes the magnetic forces in eq 1 onto the capsule shell and thus the capsule shape. Therefore, an iterative solution scheme has to be used. For a given trial shape, we calculate the magnetic field inside the capsule using only the externally applied field. Using the new field, we can recalculate the magnetic forces and a new equilibrium shape. This is iterated until shape and field converge to a fixed point. This iterative solution scheme for a ferrofluid-filled capsule has been introduced and is explained in detail in ref 18.

EXPERIMENTS AND RESULTS

Mechanical Characterization of the Capsule Shell. We first characterize the capsules mechanically and determine the two-dimensional Young modulus \( Y_{2D} \) and the surface Poisson ratio \( \nu \). These values are subsequently used in the theoretical model for magnetic deformation. We determine mechanical parameters of the shell with two independent methods, compression between parallel plates and spinning capsule deformation. If the Poisson’s ratio \( \nu \) is known both methods give the two-dimensional elastic modulus \( Y_{2D} \). A separate measurement of \( \nu \) is, however, difficult and often a generic value is assumed. By combining the results of the two independent measurements, we overcome this problem and obtain two independent equations for the two unknowns \( Y_{2D} \) and \( \nu \), which enables us to determine both quantities.

The first method, the compression between parallel plates (capsule squeezing) is a well-known technique for the mechanical characterization of capsules. A capsule is placed between two parallel plates and the force is measured as a function of the displacement. From the force–displacement compression curve, elastic moduli of the capsule shell can be calculated. There are different methods to analyze the force–displacement curves. Some methods, like the one developed by Barthès-Biesel et al., use a fit of the whole curve. As shown in an earlier publication, water leaks out of alginate capsules during compression. Therefore, we only analyze the linear regime with low forces in order to minimize the influence of water leakage.

To describe the compression of a capsule between parallel plates in the initial linear regime, the model of Reissner for a point force acting on the apex of the capsule can be used. In this model the force \( F \) depends linearly on the displacement \( d \) as

\[
F = \frac{4Y_{2D}}{R_s \sqrt{3(1 - \nu^2)}} d
\]

Reissner’s linear theory applies to an unpressurized shell with purely elastic tensions and rest radius \( R_s \). Here, we need to generalize this model to include the interfacial tension \( \gamma \), which generates a stretching tension in the shell already before indentation by the force. We find that the effect of an additional interfacial tension \( \gamma \) is equivalent to the effect of an internal pressure \( p_0 = 2\gamma/R_s \) given by the Laplace–Young equation; such pressurized capsules have been studied previously by Vella et al. in ref 10. Using this equivalence we obtain a modified linear force–displacement relation

\[
F = \frac{4Y_{2D}}{R_s \sqrt{3(1 - \nu^2)}} G(\tau) d
\]

(5)

with

\[
G(\tau) = \frac{\pi}{2} \arctanh(1 - \tau^2/3)^{3/2}
\]

(6)

\[
\tau = 3(1 - \nu^2)(\gamma/Y_{2D}^2)(R_s/p_0)^2
\]

(6)

(more details on the derivation are given in the Supporting Information). Note that a vanishing interface tension \( \gamma = 0 \) leads to \( G(\tau) = 1 \), and we recover the Reissner result (eq 4). To obtain the...
elastic moduli from this linear model, also the radius of the undeformed capsule $R_0$ and the thickness of the shell $h$ are needed.

The second method for the determination of $Y_{2D}$ and $\nu$ is the spinning capsule method. Originally, the spinning drop method was developed for interfacial tension measurements. A drop is placed in a capillary filled with a liquid of higher density $\rho$. During rotation of the capillary the drop deforms; the shape of the deformed drop depends on the rotation frequency and interfacial tension $\gamma$. For the deformation of liquid-filled capsules, Pieper et al. developed a model that allows one to obtain in an analogous fashion 2D elastic moduli from the capsule deformation. A sketch of the method is shown in the Supporting Information. Initially (at small rotation speed), the capsule is in an undeformed (quiescent) state. Then capsule deformation is measured as a function of the angular rotation frequency $\omega$. The capsule deformation is quantified by the Taylor deformation

$$D = \frac{l - b}{l + b}$$

which is determined from the length $l$ and the width $b$ of the capsule.

where $R_0$ is the radius of the undeformed capsule, $\Delta \rho$ is the density difference between the inside and outside liquid phases. Equation 8 is only valid for shells with purely elastic tensions and without an interfacial tension. Again we need to generalize the theory to include an interfacial tension $\gamma$. This can be done by observing that the linear response of the capsule deformation in spinning drop experiments is actually equivalent to the linear deformation response of a ferrofluid-filled capsule in a uniform external magnetic field with a magnetic susceptibility $\chi = -1$ and a magnetic field strength $\mu_0 H = \Delta \rho \gamma R_0^3$. This equivalence arises because both centrifugal forces exerted by the Taylor fluid in the spinning capsule and magnetic forces exerted by the ferrofluid in an external field are normal surface forces. Moreover, for a spherical shape they have the same position-dependence for $\chi = -1$ and the same magnitude if we set $\mu_0 H^2 = \Delta \rho \gamma R_0^3$. In ref 18 the deformation of a ferrofluid-filled magnetic capsule has already been considered also in the presence of an interfacial tension $\gamma$ and we can exploit the equivalence of both problems and adapt the results of ref 18 for the linear response (more details are given in the Supporting Information). We find

$$D = \frac{-\Delta \rho \omega^2 R_0}{16Y_{2D}} \frac{(S + \nu)}{R_0}$$

that is, in the presence of an interfacial tension we simply have to replace $Y_{2D}$ in eq 8 by $Y_{2D} + (S + \nu)\gamma$.

The two unknown material parameters Young’s modulus $Y_{2D}$ and surface Poisson ratio $\nu$ can now be obtained from solving the two eqs 5 and 9 simultaneously. We determined from image analysis (see Materials and Methods) as $794 \pm 87 \mu$m for the shell thickness. The shell thickness was determined by SEM (see Materials and Methods and Supporting Information). The shell thickness estimated by SEM was under $1 \mu$m. As SEM is performed in ultra-high vacuum, swelling has to be taken into account. Because we were not able to resolve the hydrated capsule shell by optical microscopy, its thickness has to be below $5 \mu$m. We conclude that the shell thickness of hydrated capsules is approximately $3 \mu$m but with a relatively high error around $1 \mu$m.

Figure 4 shows the results for the force–displacement curves in the capsule compression tests. We measured 15 individual capsules, and the respective force values for the displacement were averaged to gain information on replicability. In Figure 4 the averaged force–displacement curve is shown. The linear regime can be seen clearly. In this regime the error bars are also relatively low. Higher error bars with increasing compression are an effect of capsule size variations. For the calculation of the elastic moduli, the analysis was performed for each capsule separately with the respective radii and an average value $F_{R_0}/d$ is extracted from the linear regime (blue curve in Figure 4).

Figure 5 shows the results of the spinning capsule experiments for one exemplary capsule. Because of small mechanical forces which act during the capsule synthesis, we observed small initial Taylor deformation values of $D_i = 1−2\%$, which were not caused by deformation in the centrifugal field. Also the initial quiescent capsule state is measured at $\omega_0 > 0$. Therefore, we subtract the initial deformation and initial angular frequency and use the Taylor deformation difference $\Delta D = D - D_i$ and the difference $\Delta \omega = \omega - \omega_0$ for the analysis. Figure 5 shows the expected linear dependence of $\Delta D$ from the parameter $\Delta (\Delta \rho \omega^2 R_0^3)$ according to eq 9. The deviations at higher rotation frequencies are caused by water leakage from the capsule, which was also observed in previous studies. For the calculation of the elastic moduli, the slope $\Delta D/\Delta (\Delta \rho \omega^2 R_0^3)$ is determined from the initial linear regime (blue curve in Figure 5).

The results from both capsule deformation methods are used to calculate the surface Poisson ratio $\nu$ and the 2D Young modulus $Y_{2D}$ by solving eqs 8 and 9 simultaneously. We find

$$Y_{2D} = 0.186 \pm 0.040 \text{ N/m}$$

and

$$1 - \nu = (1.9 \pm 2.8) \times 10^{-7}$$

Because $\nu$ is extremely close to unity, the two eqs 5 and 9 can be decoupled with negligible error, which leads to the following simplification: we set $\nu = 1$ in eq 9 and calculate $Y_{2D}$ from eq 9 only from the spinning capsule experiment. This value is then used to calculate $\nu$ via eq 5. This decoupling has the additional benefit that we can determine $Y_{2D}$ from eq 9 for the spinning capsule experiment effectively independently of the shell thickness $h$, which can only be measured with a relatively high error as explained above.

As compared to other calcium alginate capsules, the moduli are very low. This is likely an effect of the encapsulated components, that is, the nanoparticles or the specific oils used. In emulation
encapsulation, the moduli were lowered by the addition of nanoparticles. As the main goal was to obtain easily deformable capsules, this was achieved by creating very thin shells. A remarkable result is the high surface Poisson ratio, which points to an area-incompressible shell. Therefore, we further check this finding by adjusting this parameter in the numerical calculation and analysis of the magnetic deformation of the capsule shape to fit the experimental shapes. For Young’s modulus we use the measured value $Y_{2D} = 0.186$ N/m in the numerical calculations (see Table 1).

**Magnetic Deformation.** We prepared different capsules and deformed them with the previously described inhomogeneous field by increasing the electric current in the coil up to 5 A. This corresponds to magnetic field variations up to 50 mT over the size of the capsule. Photos of three exemplary capsules that have reached their steady state of deformation are shown in Figure 6. In Figure 6 we compare these photos with numerically calculated contours (with dashed lines), which were generated with the parameter values in Table 1. These are the experimentally measured parameter values except for the surface Poisson ratio $\nu$. In particular, we consider the mechanical measurements of the Young modulus $Y_{2D} = 0.186$ N/m to be exact and employ this value in the numerics. The Poisson ratio $\nu = 1 - 1.9 \times 10^{-4}$ from mechanical characterization is extremely close to unity; it depends very sensitively on the shell thickness $b$, which is not easy to determine reliably. Therefore, we regarded $\nu$ as a free parameter and adjusted $\nu$ for the best fit to the experimental shapes, which gives a slightly lower value $\nu \approx 0.946$. This confirms that the surface Poisson ratio of the shell is close to unity.

There are minor deviations between experimental capsule shapes and the calculated contours, which are probably caused by inhomogeneities and asymmetries in the shell thickness. In addition, we also observe in Figure 6 that a small amount of transparent liquid is pushed to the upper part of the capsule. Therefore, the behavior of the whole capsule should be comparable to a capsule with only a ferrofluid inside.

In order to perform a quantitative comparison between numerics and the experiment, we measure the ratio of the capsule’s height ($a$) to the maximum width ($b$), measured parallel to the plate below the capsule. The results of these measurements are shown in Figure 8. We achieve the best agreement between numerical calculations and experimental data for $\nu \approx 0.946$. As also the comparison of capsule shapes in Figure 6 indicates, there is a good agreement between numerical calculations and the experiment for $\nu \approx 0.946$. The only point with some higher deviation is at $I = 0$, that is, in the absence of any magnetic field. Then the deformation of the capsule is only caused by gravity and, thus, is in total relatively small. This makes the capsule side ratio $a/b$ very prone to asymmetries of the shell. In addition, the capsule is not a perfect sphere after membrane gelation as it is assumed in the numerical calculation.

We can also check that the capsule’s volume $V_0$ remains constant during the magnetic deformation process. Any loss of the inner liquid through the shell would be visually detectable during contact with the outer fluid. In addition, analysis of the capsule photos for the capsule contour $r(z)$ and calculation of the volume $V_0 = \int dz r^2(z)$ does not indicate any loss of volume (see Supporting Information). We conclude that the elastic shell is impermeable for the inner and outer fluid under the employed experimental conditions and during magnetic deformation.

An important characteristic for possible applications is the question if the material is weakened by the deformation, that is, whether aging effects occur. We checked this by performing a second deformation cycle. The results are shown in Figure 9 exemplarily for the first capsule. Second and first deformation cycles agree well which indicates that no significant damage or aging in the elastic shell occurs during the deformation process. Also the preserved volume during deformation hints at a reversible deformation process.

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**Figure 7.** Magnified photographic image of capsule 1 for $I = 5$ A. A non-magnetic transparent liquid, which is clearly phase-separated from the ferrofluid, is pushed to the upper part of the capsule.

**Figure 8.** Ratio of capsule height $a$ to width $b$ for increasing current $I$. Markers denote capsules from the experiment, while solid lines represent numerical data generated with the best fit $\nu \approx 0.946$. The upper curve (blue, squares) are data for capsule 1 from Figure 6, the middle curve (red, triangles) and lower curve (green, circles) data for capsules 3 and 2, respectively.
Having established a good agreement between experiment and theory as evidenced by Figures 6 and 8, we can use the theoretical model to access important physical quantities that are experimentally hardly accessible, such as the detailed distributions of magnetic field and stresses. The distribution of the magnetic field inside the deformed capsules is easy to calculate from our model. Figure 10 shows the magnetic field inside and outside of capsule 1 at \( I = 5 \) A, the stray field generated by the magnetized capsule, and the magnetization inside the capsule. The external magnetic field has a high gradient, but the total field inside the capsule is surprisingly homogenous. The magnetization of the ferrofluid decreases the total field in the lower section of the capsule, whereas it increases the total field in the upper part because it counteracts the external magnetic field according to Lenz’s law. This results in smaller field gradients inside the capsule. Magnetization variations inside the capsule are small.

Also the elastic stress state inside the elastic shell as given by the stress and strain distribution becomes accessible by numerical calculation. Figure 11 shows the force/stress/strain distribution along the capsule contour for capsule 1 in different stages of deformation. The position of the highest elastic stress is marked, which is at the highly curved region at the bottom of the capsule. We can infer that the capsule will most likely rupture at this position if the magnetic field is further increased.

**Poisson’s Ratio** \( \nu \). For the numerics, we consider the measurement of the Young modulus to be exact with a value of \( Y_{2D} = 186 \) N/m. Varying the surface Poisson ratio \( \nu \), we find the best match between numerics and experiment for \( \nu \approx 0.946 \). This confirms a surface Poisson ratio of the shell very close to unity and is only slightly lower than the value \( \nu = 1 - 1.9 \times 10^{-7} \) from mechanical characterization. This represents an explicit measurement of the surface Poisson ratio for an alginate membrane. Other measurements of the surface Poisson ratio of alginate shells are only available for barely comparable systems and solely rely on mechanical characterization; in the literature often a generic value (such as \( \nu = 1/3 \) or \( \nu \approx 0.5 \)) is assumed.

The two-dimensional area compression modulus \( K_{2D} = Y_{2D}/2(1 - \nu) \) diverges for \( \nu \) close to unity. Therefore, surface Poisson ratios close to unity are remarkable as they imply a polymerized shell that is nearly area preserving during deformation. For Poisson ratios \( \nu \) close to unity, strong elastic deformations also become quite sensitive to changes of \( \nu \), as the diverging compression modulus also gives rise to diverging elastic stresses containing factors \( 1/(1 - \nu) \). This allows us to determine \( \nu \) rather precisely by fitting numerical to experimental shapes (see also Supporting Information).

In a three-dimensional material volume-incompressibility during deformation corresponds to a three-dimensional Poisson ratio \( \nu_{3D} = 0.5 \) (the three-dimensional compression modulus is \( K_{3D} = Y_{3D}/3(1 - 2\nu_{3D}) \)). Three-dimensional Poisson ratios close to \( \nu_{3D} = 0.5 \) are common for three-dimensional polymeric materials, where volume-incompressibility is, for example, explicitly implemented in the Mooney–Rivlin constitutive relation commonly used for polymeric materials. For polymeric materials incompressibility can be attributed to the effectively incompressible densely packed liquid of monomers. Also alginate gels are typically regarded as volume-incompressible materials as confirmed by measurements, for example, in refs 53 and 54. A material that is volume-incompressible in three dimensions (\( \nu_{3D} = 0.5 \)) forms an area-incompressible thin shell if the shell has constant thickness during deformation. If the thickness can adapt, on the other hand, we expect \( \nu = \nu_{3D} = 0.5 \) and the thickness grows (shrinks) if the shell area is compressed (expanded). Therefore, our findings are consistent with an alginate shell consisting of a volume-incompressible material that maintains a shell of constant thickness during deformation. It remains to be clarified whether the inherently anisotropic structure of the alginate gel which results from the ionotropic gelation process\(^{30} \) can contribute to the observed high surface Poisson ratios. From a chemical point of view, we expect the Poisson number to depend on the cross-linking and swelling degree of the encapsulating alginate membranes.

**CONCLUSIONS**

Ferrofluids are an interesting tool for different applications involving the actuation of a fluid by magnetic fields. The encapsulation of the ferrofluid can prevent the interaction of the fluid with its environment. In this work, we presented a novel method to encapsulate a ferrofluid drop with a very thin elastic shell.

Using this method, a direct encapsulation of oils in alginate gels could be achieved. We used 1-hexanol as an additive to directly dissolve CaCl\(_2\) for ionotropic gelation of sodium alginate in an organic solvent. The magnetic nanoparticles remained stable throughout the whole process and formed a stable ferrofluid. The produced elastic capsules showed low Young moduli, especially compared to other calcium alginate gels. This enables a strong deformation in relatively weak magnetic fields, which opens possibilities for applications as, for example, switches or valves in confined spaces like microfluidic devices. In these applications, it is essential to

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**Figure 10.** Numerically calculated distributions of magnetic field strength (left), stray field (middle), and magnetization (right) for capsule 1 (see Figure 6) at \( I = 5 \) A. The solid line represents the capsule’s elastic shell. Left: Color codes for the absolute value of the total magnetic field \( |\mathbf{H}| \) (in A/m). Middle: Color codes for the absolute value of the own magnetic stray field \( H_{\text{stray}} = H - H_{\text{magnet}} \) (in A/m), arrows indicate the field direction. Right: Color codes for the absolute value of the magnetization \( |\mathbf{M}| \) (in A/m). Note that magnetization variations are very small.
protect the components from contact with the ferrofluid, as it is likely to cause unwanted reactions due to its high reactivity. Concerning a transfer to the biological or medical sector as motion-controllable and deformable capsule systems, applications in micromanipulation are imaginable. For any sort of industrial or medical application, a change of the system is necessary as chloroform is a highly volatile and toxic compound. This is, however, easily achieved as the oil is exchangeable and chloroform was only used because of its high density. It is also likely that the 1-hexanol can be substituted by other alcohols.

We first characterized the capsules mechanically using a combination of compression and spinning capsule techniques. We produced nearly spherical capsules with radii about \( R_0 = 1 \) mm and mechanical characterization showed a two-dimensional Young modulus of \( Y_{2D} = 0.186 \) N/m. The surface Poisson ratio was close to unity.

Then we performed magnetic deformation in an inhomogeneous field in front of a hard constraining wall. Our results in Figure 8 demonstrate that high deformations with height to width ratios as low as 0.6 could be achieved in inhomogeneous magnetic fields which vary by 50 mT over the size of the capsule. Maximal strains of about 17% occur in the capsule shell during deformation (see Figure 11). The volume inside the capsules was constant during magnetic deformation, that is, the alginate shells were impermeable. The inclusion of a nonmagnetic, transparent, water-based liquid inside every capsule was observed. Moreover, magnetic deformation was shown to be completely reversible over several deformation cycles without plastic or aging effects.

We presented a theoretical model and a numerical method to predict the deformation behavior in magnetic fields by numerical calculations using parameter values from the experimental characterization as input parameters. The comparison of the capsule deformation with numerical calculations based on a nonlinear small strain shell theory showed a good agreement between theory and experiment (see Figures 6 and 8). In the numerical calculations we used the surface Poisson ratio \( \nu \), which is notoriously hard to measure experimentally, as a fit parameter, which was adjusted to optimally fit experimental shapes. In agreement with the mechanical characterization we obtained values \( \nu \) close to unity (\( \nu = 0.946 \)). Therefore, our results constitute the first reliable measurement of the surface Poisson ratio of alginate gel capsule shells. Surface Poisson ratios close to one suggest that the alginate shell deforms nearly area-preserving. The molecular reasons for this behavior remain to be clarified.

Having established the agreement between the theoretical model and experimental results, we can use the numerical results to gain further insight into details of the deformation behavior, which are not experimentally accessible. The numerical approach gives access, for example, to the complete magnetic field distribution inside and outside the ferrofluid-filled capsule, the exerted magnetic forces, the stress distribution, and the exact deformation state in terms of strains, see Figures 10 and 11.

**ASSOCIATED CONTENT**

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.langmuir.8b02357.

Additional details on shape equations, on the theory of spinning drop and capsule compression analysis in the presence of an interfacial tension \( \gamma \), and on the sensitivity of capsule deformation to Poisson number \( \nu \). Details on the spinning drop and capsule compression experiments, the image analysis for radius and volume measurements, the SEM measurements of capsule thickness, the fit of the magnetic field distribution, and on the dynamic light scattering to determine magnetic nanoparticle size distributions. List of chemicals (PDF)

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